

$$t = \int_0^z \frac{dz}{w} = \frac{9a}{10} \left( \frac{18aF_0}{5\pi} \right)^{-\frac{1}{3}} z^{\frac{4}{3}}$$