



Figure 2: Merging Gaussian functions for a unit sources separation. (Kaye and Linden, 2004)

where  $z$  is the height above the plume sources (vertical origins),  $\xi_0$  the separation of the plume sources,  $\xi$  the separation of the plume axes at any given height, and  $b$  the plume radius.

Consider the two equal plumes with origins at the same height. The average buoyancy profile of a single turbulent plume can be taken as Gaussian, with a radius given by

$$b = \frac{6}{5}\alpha z, \quad (27)$$

where  $\alpha$  is the entrainment constant. Assuming that the plumes do not interact, buoyancy profile function is given by

$$g'(r, z) \sim f(z)E(r), \quad (28)$$

$$E(r) = \exp\left[-\frac{(r - \frac{1}{2}\xi_0)^2}{b^2}\right] + \exp\left[-\frac{(r + \frac{1}{2}\xi_0)^2}{b^2}\right]. \quad (29)$$

Here  $r$  is the radial distance from the plume axis and  $g'$  is the reduced gravity.

This function (28) is plotted in figure 2 for  $1 < \lambda < 8$  and  $x_0 = 1$ . Clearly the two Gaussians coalesce when  $\lambda$  is large enough. We define the merging height to be the height at when the trough in the combined profile disappears, that is,

$$\frac{d^2 E}{dr^2} = 0 \quad \text{at} \quad r = 0. \quad (30)$$

For non-interacting plumes (i.e.  $\xi(z) = x_0$ ), (30) is easily solved to give

$$\xi_0 = \sqrt{2}b_m. \quad (31)$$

Here the subscript  $m$  denotes the value at the point where plumes merge. Dividing (31) by  $\xi$ , we obtain

$$\gamma_m = \frac{1}{\sqrt{2}}, \quad (32)$$